

B. The C_n Groups

C_2	E	C_2			
A	1	1	z, R_z	x^2, y^2, z^2, xy	$z^3, xyz, z(x^2 - y^2)$
B	1	-1	x, y, R_x, R_y	yz, xz	$xz^2, yz^2, x(x^2 - 3y^2), y(3x^2 - y^2)$

C_3	E	C_3	C_3^2	$\varepsilon = \exp(2\pi i/3)$		
A	1	1	1	z, R_z	$x^2 + y^2, z^2$	$z^3, x(x^2 - 3y^2), y(3x^2 - y^2)$
E	$\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$	$(x, y), (R_x, R_y)$		$(x^2 - y^2, xy), (yz, xz)$	$(xz^2, yz^2), [xyz, z(x^2 - y^2)]$	

C_4	E	C_4	C_2	C_4^3			
A	1	1	1	1	z, R_z	$x^2 + y^2, z^2$	z^3
B	1	-1	1	-1		$x^2 - y^2, xy$	$xyz, z(x^2 - y^2)$
E	$\begin{cases} 1 & i \\ 1 & -i \end{cases}$	$(x, y), (R_x, R_y)$			(xz, yz)	$(xz^2, yz^2), [x(x^2 - 3y^2), y(3x^2 - y^2)]$	

C_5	E	C_5	C_5^2	C_5^3	C_5^4	$\varepsilon = \exp(2\pi i/5)$		
A	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$	z^3
E_1	$\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$	ε^2	ε^{2*}	ε	$(x, y), (R_x, R_y)$	(yz, xz)	(xz^2, yz^2)	
E_2	$\begin{cases} 1 & \varepsilon^2 \\ 1 & \varepsilon^{2*} \end{cases}$	ε^*	ε	ε^{2*}		$(x^2 - y^2, xy)$	$[xyz, z(x^2 - y^2)], [x(x^2 - 3y^2), y(3x^2 - y^2)]$	

C_6	E	C_6	C_3	C_2	C_3^2	C_6^5	$C_6 = C_3 \times C_2$	$\varepsilon = \exp(2\pi i/6)$		
A	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$	z^3	
B	1	-1	1	-1	1	-1			$x(x^2 - 3y^2), y(3x^2 - y^2)$	
E_1	$\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$	$-\varepsilon^*$	-1	$-\varepsilon$	ε^*		$(x, y), (R_x, R_y)$	(xz, yz)	(xz^2, yz^2)	
E_2	$\begin{cases} 1 & -\varepsilon^* \\ 1 & -\varepsilon \end{cases}$	$-\varepsilon$	1	$-\varepsilon^*$	$-\varepsilon$			$(x^2 - y^2, xy)$	$[xyz, z(x^2 - y^2)]$	

C_7	E	C_7	C_7^2	C_7^3	C_7^4	C_7^5	C_7^6	$\varepsilon = \exp(2\pi i/7)$			
A	1	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$	z^3	
E_1	$\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$	ε^2	ε^3	ε^{3*}	ε^{2*}	ε^*		$(x, y), (R_x, R_y)$	(xz, yz)	(xz^2, yz^2)	
E_2	$\begin{cases} 1 & \varepsilon^2 \\ 1 & \varepsilon^{2*} \end{cases}$	ε^3	ε^*	ε	ε^*	ε^{3*}	ε^2		$(x^2 - y^2, xy)$	$[xyz, z(x^2 - y^2)]$	
E_3	$\begin{cases} 1 & \varepsilon^3 \\ 1 & \varepsilon^{3*} \end{cases}$	ε^*	ε^2	ε^{2*}	ε	ε^{3*}				$[x(x^2 - 3y^2), y(3x^2 - y^2)]$	

C_8	E	C_8	C_4	C_2	C_4^3	C_8^3	C_8^5	C_8^7	$C_8 = C_4 \times C_2$	$\varepsilon = \exp(2\pi i/8)$		
A	1	1	1	1	1	1	1	1	z, R_z	$x^2 + y^2, z^2$	z^3	
B	1	-1	1	1	1	-1	-1	-1				
E_1	$\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$	i	-1	$-i$	$-\varepsilon^*$	$-\varepsilon$	ε^*		$(x, y), (R_x, R_y)$	(xz, yz)	(xz^2, yz^2)	
E_2	$\begin{cases} 1 & i \\ 1 & -i \end{cases}$	-1	1	-1	-1	i	i	$-i$		$(x^2 - y^2, xy)$	$[xyz, z(x^2 - y^2)]$	
E_3	$\begin{cases} 1 & -\varepsilon \\ 1 & -\varepsilon^* \end{cases}$	i	-1	$-i$	$-\varepsilon^*$	ε	ε^*	$-\varepsilon^*$			$[x(x^2 - 3y^2), y(3x^2 - y^2)]$	